



# **INVENTORY MANAGEMENT**

#### • GOAL:

Find the right balance between the **supply** and **de**mand of products by optimizing replenishment decisions and minimizing costs.

### • **BENEFITS**:

- $\hookrightarrow$  Better inventory accuracy
- $\hookrightarrow$  Insights to cost savings
- $\hookrightarrow$  Avoidance of stock-outs

### • FRAMEWORK:

A controller observes the past demands and local information of the inventory and has to decide about the next ordering values.

• MAIN ISSUE: Environment uncertainty

 $\hookrightarrow$  demands and lead-times are stochastic with potentially high volatility.

 $\hookrightarrow$  controller may exceedingly order, leading to unnecessary *ordering* and *holding* costs.

 $\hookrightarrow$  controller may insufficiently order, leading to *shortage* costs and may jeopardize the company's performance.

# CONTRIBUTIONS

(1) We develop a novel reinforcement learning framework, called **MARLIM**, to address the inventory management problem for a single-echelon multi-products supply chain on a production line with stochastic demands and lead-times.

(2) We provide the methodology to train agents in different scenarios for fixed or shared capacity constraints with specific handling of storage overflows.

(3) We perform various numerical experiments on realworld data to demonstrate the benefits of our method over classical baselines.



# MARLIM: Multi-Agent Reinforcement Learning for Inventory Management

Rémi Leluc<sup>1</sup>, Elie Kadoche<sup>2</sup>, Antoine Bertoncello<sup>2</sup>, Sébastien Gourvénec<sup>2</sup> LTCI, Télécom Paris, Institut Polytechnique de Paris, <sup>2</sup>TotalEnergies OneTech

### **INVENTORY COSTS**

For any item  $i \in \mathcal{N}$ , denote by  $C_o^{(i)}, C_h^{(i)}$  and  $C_s^{(i)}$  the unit ordering, holding and shortage costs respectively.

(a) **Ordering costs**: functioning costs, reception costs, salaries personnel, labor costs, rent of a factory, energy consumption allocated for production.

(b) Holding costs: financial and functional costs, rent and maintenance of required space, insurance costs, transportation and obsolescence costs.

(c) **Shortage costs**: demand exceeds available inventory  $\hookrightarrow$  backlogging costs and penalty shortage cost.

# **INVENTORY DYNAMICS**

At time *t*, for each product i = 1, ..., n, inventory controller decides about the order  $a_t^{(i)}$  to take based on the current inventory level  $x_t^{(i)}$  and the stochastic demand  $\delta_t^{(i)}$ . Order arrives after stochastic lead-time  $\tau_t^{(i)}$ .

tem <i>i</i> , time <i>t</i>	take order	$ au_{\star}^{(i)}$ .	update
level $x_t^{(i)}$	$\rightarrow$ action $a_t^{(i)}$	lead-time	orders list
$\oint t \leftarrow t + 1$			
$(x_{t+1}^{(i)}, \beta_{t+1}^{(i)})$ update			receive quantity $\rho_t^{(i)}$

After receiving replenishment quantity  $\rho_t^{(i)}$  the inventory levels are temporarily updated through  $\lambda_t^{(i)} =$  $x_t^{(i)} + \lfloor w_t^{(i)} \rho_t^{(i)} \rfloor$ . The levels and backlogs  $\beta_t$  are updated to evaluate the inventory costs  $C_t^{(i)}$ .

$$\begin{aligned} x_{t+1}^{(i)} &= \left(\lambda_t^{(i)} - \delta_t^{(i)}\right)_+ \quad \beta_{t+1}^{(i)} = \beta_t^{(i)} + \left(\lambda_t^{(i)} - \delta_t^{(i)}\right)_+ \\ C_t^{(i)} &= \alpha_o \underbrace{a_t^{(i)} C_o^{(i)}}_{\text{ordering}} + \alpha_h \underbrace{x_t^{(i)} C_h^{(i)}}_{\text{holding}} + \alpha_s \underbrace{\beta_{t+1}^{(i)} C_s^{(i)}}_{\text{shortage}} \end{aligned}$$

where  $\alpha_o, \alpha_h, \alpha_s \in [0, 1]$  with  $\alpha_o + \alpha_h + \alpha_s = 1$ are weighting coefficients that translate some expert's knowledge about the desired strategy.

#### **INVENTORY FEATURES**

• warehouse with *n* independent products (one agent per item). capacity of each product is either: (1) finite and non-variable for each product (single agents) or (2) shared with finite capacity in cluster (multi-agents RL). • stochastic demands and lead-times (e.g. Poisson, Geometric) with stationary distributions that may be infered from historical data.

• The inventory costs of each agent are associated to the single reward defined as:  $r^i(s_t, a_t) = -C_t^i$ . Inside a product subspace  $\mathcal{N}_k$ , the agents are working in a cooperative setting in order to optimize the average reward  $r_k(s_t, a_t) = \sum_{i \in \mathcal{N}_k} r^i(s_t, a_t) / |\mathcal{N}_k|$ .

#### NUMERICAL DETAILS

operation research. action space.

#### NUMERICAL RESULTS





**Figure 1:** Inventory level (*blue*) over T = 120 months: MinMax (left), Oracle (center), PPO (right). The demand is plotted in *red* and the order actions are plotted in *green*. The safety stock MinMax agent is displayed in *orange*.



**Figure 2:** Learning curves of clusters  $\mathcal{N}_1, \mathcal{N}_2$  and  $\mathcal{N}_3$  where the mean and standard deviation of IPPO are plotted in *blue* and the horizontal lines are average reward for baselines Oracle (green) and MinMax (red) computed over 100 replications.



**Figure 3:** Average Cumulative Costs and Item Shortages obtained over 100 replications, horizon T = 240 months for Items 0-9.



• Lead-time geometric  $\tau^{(i)} \sim \mathcal{G}(p_i)$ .

• Demand  $\delta^{(i)} \sim X_i Y_i$  with  $X_i \sim \mathcal{B}(b_i), Y_i \sim \mathcal{P}(\mu_i)$ .

*MinMax agents*: a standard min-max strategy (s, S) from

*Oracle agents*: order at each time according to a normal law  $\mathcal{N}(\hat{\mu}_{\delta}, \hat{\sigma}_{\delta}^2)$  which is clamped to fit the bounds of the

MARL agents: PPO algorithm, when working with capacity constraints per item, both discrete and continuous policies are considered, denoted by PPO-D and PPO-C respectively. When the items compete for storage space, we implement IPPO.